(Following Paper ID and Roll No. to be filled in your Answer Book)
PAPER ID: 199222 Roll No.

### B.Tech.

# (SEM. II) THEORY EXAMINATION 2013-14

### **ENGINEERING MATHEMATICS-II**

**EAS203** 

(Following Paper ID and Roll No. to be filled in your Answer Book)
PAPER ID: 199208 Roll No.

### B.Tech.

## (SEM. II) THEORY EXAMINATION 2013-14

### **ENGINEERING MATHEMATICS-II**

Time: 3 Hours

Total Marks : 100

Note: - Attempt all questions.

### SECTION-A

1. Attempt all parts of this question:

 $(10 \times 2 = 20)$ 

(a) Solve 
$$\frac{d^3y}{dx^3} + 2\frac{d^2y}{dx^2} + \frac{dy}{dx} = 0$$
.

- (b) Find the particular integral of  $(D^2 4D + 4)y = \cos 2x$ .
- (c) Evaluate  $\int_{-1}^{1} x^3 P_2(x) dx$
- (d) Find the values of m and n for which

$$\int_0^1 x J_0^2(\alpha x) dx = \frac{1}{2} \left[ J_n(\alpha) \right]^2.$$

- (e) Find the Laplace transform of unit step function u(t).
- (f) Find the inverse Laplace transform of  $F(s) = \frac{3}{s^2 + 2s \theta}$ .
- (g) If f(x) = 1,  $0 < x < \pi$  is expanded in half range cosine series then find the value of  $a_0$ .
- (h) Solve r t + p q = 0.
- (i) Classify the following partial differential equation along the line y = x:

$$y u_{xx} + (x + y) u_{xy} + x u_{yy} = 0.$$

(j) Find the steady state temperature distribution in a rod of length 20 cm, whose ends are kept at 0°C and 60°C.

### SECTION-B

- 2. Attempt any three parts of the following: (3×10=30)
  - (a) An RCL circuit connected in series with an inductance of 1 henry, a resistance of 16 ohms and a capacitance of 0.01 farad has an applied voltage of 10 sin 10 t volts. Find an expression for the current through the circuit at any time t if there is no initial current and no initial charge on the capacitor.
  - (b) Find the Frobenius series solution of the following differential equation about x = 0:

$$(1-x^2)v''-xv'+4v=0.$$

(c) Apply Laplace transform technique to solve:

$$\frac{d^2x}{dt^2} + 16x = 2\sin 4t, \ \ x(0) = -\frac{1}{2}, \ x'(0) = 0$$

2

(d) Find the Fourier series expansion of the following function:

$$f(x) = \begin{cases} 0, & -\pi < x \le 0 \\ x, & 0 \le x < \pi \end{cases}$$

Hence find the sum of the series  $\sum_{n=1}^{\infty} \frac{1}{(2n-1)^2}.$ 

(e) The initial temperature distribution in a square plate of unit length is 100°C. Find the temperature distribution u(x, t) if all the sides are maintained at zero degree temperature.

- 3. Attempt any two parts of the following:  $(2\times5=10)$ 
  - (a) Solve  $\frac{d^2y}{dx^2} 2\frac{dy}{dx} + y = x^2 e^{3x}$ .
  - (b) Use method of variation of parameter to find the particular integral of:

$$\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} + 4y = \sec 2x.$$

(c) Solve:

$$\frac{dx}{dt} = -4(x+y); \quad \frac{dx}{dt} + 4\frac{dy}{dt} = -4y$$

with conditions x(0) = 1, y(0) = 0.

- 4. Attempt any two parts of the following: (2×5=10)
  - (a) Prove that  $J_{n-1}(x) + J_{n+1}(x) = \frac{2n}{x} J_n(x)$ . Hence compute  $J_{3/2}(x)$ .
  - (b) Prove that  $nP_n(x) = xP_n'(x) P_{n-1}'(x)$ .
  - (c) Find the Fourier-Legendre expansion upto p<sub>3</sub>(x) for the following function:

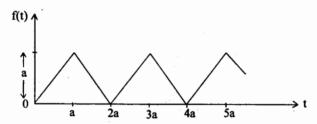
3

$$f(x) = \begin{cases} 0, & -1 < x < 0 \\ 1, & 0 < x < 1 \end{cases}$$

- (a) Find the Laplace transform of  $\int_0^t \frac{\cos 2t \cos 3t}{t} dt$ .
- (b) Find the function whose Laplace transform is:

$$F(s) = \log \frac{s^2 + 1}{s(s+1)}$$

(c) Find the Laplace transform of the periodic function shown in the figure:



- 6. Attempt any two parts of the following: (2×5=10)
  - (a) Solve  $y^2p xyq = x(z 2y)$
  - (b) Solve  $(D^2 DD' 2D'^2)$   $z = (y 1)e^x$ .
  - (c) Find the half range sine series for  $f(x) = x + x^2$ , 0 < x < 1.
- 7. Attempt any one part of the following:  $(1\times10=10)$ 
  - (a) Apply method of separation of variables to solve

$$\frac{\partial z}{\partial x} + \frac{\partial^2 z}{\partial y^2} = 0$$

satisfying the conditions z(x, 0) = 0,  $z(x, \pi) = 0$ ,  $z(0, y) = 4 \sin 3y$ .

(b) Find the deflection of the vibrating string which is fixed at the ends x = 0 and x = 2 and the motion is started by

displacing the string into the form  $\sin^3\left(\frac{\pi x}{2}\right)$  and releasing it with zero initial velocity.